CO Adsorption on Supported Gold Nanoparticle Catalysts: Application of the Temkin Model

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CO Adsorption on Supported Gold Nanoparticle Catalysts: Application of the Temkin Model

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ABSTRACT: The adsorption of CO on the supported gold nanoparticle catalysts Au/TiO2, Au/Fe2O3, and Au/ZrO2 was examined using infrared transmission spectroscopy to quantify the isobaric CO coverage as a function of temperature. The Temkin adsorbate interaction model was then applied to account for the adsorption behavior. To test the general applicability of the Temkin model, this treatment was also applied to three data sets from the literature. This included another real-world catalyst and two model catalysts. All data sets were accurately represented by the Temkin adsorbate interaction model. The resulting thermodynamic metrics are consistent with previous determinations and reflect a particle size-dependence. In particular, the intrinsic adsorption enthalpy at zero CO coverage varies almost linearly with Au particle size, and this trend appears to be correlated with the abundance of low-coordinate Au sites (cf., CN = 6 and 7 for corners and edges, respectively). For very small particles with mostly CN = 6 corner sites, the enthalpy reflects strong binding (cf., $\Delta H_0 \approx 78$ kJ/mol), while for large particles with mostly CN = 7 edge sites, the enthalpy reflects weaker binding (cf., $\Delta H_0 \approx 63$ kJ/mol). The results also suggest that these sites are coupled. This study demonstrates that the Temkin adsorbate interaction model accurately represents adsorption data, yields meaningful metrics that are useful for characterizing nanoparticle catalysts, and should be applicable to other adsorption data sets.

INTRODUCTION

Of all of the reactions examined on supported metal nanoparticle catalysts, the oxidation of CO has received extensive experimental and theoretical attention.1 While the reaction may appear to be rather straightforward, an understanding of the mechanism has been surprisingly difficult to achieve. Not only is the oxidation of CO a model system to study, but the adsorption of CO on gold, a fundamental step in the mechanism, has also become a model interaction to investigate.1

Multiple studies indicate that CO is only weakly chemisorbed on gold. The adsorption is believed to involve low-coordinate sites with coordination number CN = 6 (i.e., corners or kinks) and CN = 7 (i.e., edges or steps).2–15 Adsorption to terrace sites with CN = 8 or 9 does not occur.16 CO adsorption studies also display a number of coverage-dependent results. For example, quantification of the coverage with CO pressure (or with temperature) reveals coverage-dependent, non-Langmuir behavior.17–21 The adsorption enthalpy shows a coverage-dependence, decreasing with increasing coverage.17–24 Also, the infrared studies reveal a common CO peak that typically red shifts with increasing coverage.25–28

To account for the physicochemical, coverage-dependent behavior of CO adsorption on gold, we developed a treatment of the Temkin adsorption model.29 This thermodynamic model is an extension of the Langmuir adsorption model that incorporates a linear variation in binding energy with coverage, and has three cases that are similar but not equivalent. The adsorbate interaction case takes into account direct adsorbate–adsorbate interactions or indirect adsorbate–substrate interactions. This case assumes that these interactions produce a linear variation of adsorption enthalpy with adsorbate coverage. In contrast, the heterogeneous surface case assumes a uniform distribution of heterogeneous binding sites. It is assumed that the adsorption enthalpy varies linearly over these different binding sites. The third case involves a common approximation for midrange adsorbate coverage. According to this approximation, the expressions for the adsorbate interaction and the heterogeneous surface cases are simplified, producing a new common expression. This common expression is the familiar Temkin isothermal result; coverage varies with the logarithm of pressure.

Previously, we demonstrated that this treatment of the Temkin adsorption model provides meaningful thermodynamic metrics for enthalpy and entropy, which can be used to characterize and explain differences between various catalysts.29 The model is straightforward and applicable for fitting both isothermal and isobaric data sets.

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We now report the results of new CO adsorption studies on the real-world catalysts Au/TiO$_2$, Au/Fe$_2$O$_3$, and Au/ZrO$_2$. Infrared transmission spectroscopy was used for quantitatively measuring the adsorption coverage under isobaric experimental conditions. The coverage as a function of temperature was fit with the Temkin adsorption model that was previously developed.²⁹ The resulting thermodynamic adsorption metrics (cf., the adsorption enthalpy at zero and full coverage, and the adsorption entropy) are in excellent agreement with previously reported values. Further validation of this new Temkin treatment was also achieved by fitting literature data for CO adsorption on another real-world Au/TiO$_2$ catalyst, and on two model Au/TiO$_2$ catalysts. The data are very well represented by the Temkin adsorbate interaction model. The resulting adsorption enthalpy at zero coverage shows a nearly linear trend with Au particle size. This trend appears to be correlated with the abundance of low-coordinate Au sites (cf., CN = 6 and 7 for corners and edges, respectively).

**TEMKIN ADSORPTION MODEL**

Because the Temkin adsorption model with its three cases was previously developed in detail, only a brief review of the important expressions will be presented.²⁹ The Temkin model is an extension of the Langmuir model that incorporates a linear variation of the adsorption energy. The relevant Langmuir expressions are:

\[ \theta = \frac{K_T P}{1 + K_T P} \]  
\[ P = \frac{1}{K_T S_{\text{max}}} + \frac{P}{S_{\text{max}}} \]  

where \( \theta \) is the normalized coverage, \( K_T \) is the binding constant, \( P \) is the equilibrium pressure, \( S \) is the measured coverage at \( P \), and \( S_{\text{max}} \) is the maximum coverage. Equation 2 is the linear form of the Langmuir isotherm and is used to determine \( S_{\text{max}} \) for normalizing the coverage (cf., \( \theta = S/S_{\text{max}} = 0-1 \)).

The Temkin adsorbate interaction case assumes (i) a uniform distribution of equivalent binding sites, and (ii) the binding energy on each of the all sites varies linearly with coverage due to adsorbate interactions. The surface is uniform, meaning that all binding sites are equivalent with the same intrinsic binding energy in the absence of adsorbate interactions. The interactions can be direct adsorbate–adsorbate interactions involving the coupling of adsorbate dipoles (also called dipole–dipole coupling, or dynamic interaction) or indirect adsorbate–substrate interactions involving electronic interaction with the binding surface (also called chemical interaction). The coverage \( \theta \) has the same meaning as in the Langmuir model, but \( K_T \) is allowed to vary with coverage due to a linear change in \( \Delta H \) with coverage, according to:

\[ \Delta H_\theta = \Delta H_0 - \delta \Delta H \quad \text{where} \quad \delta \Delta H = \Delta H_0 - \Delta H_1 \]  

All enthalpy terms are negative, \( \Delta H_0 \) and \( \Delta H_1 \) are the enthalpies at zero and full coverage, and \( \theta \) goes from 0 to 1. The relevant coverage-dependent expressions for the Temkin adsorbate interaction case are then:

\[ \Delta G_{\theta,T} = -RT \ln \left( \frac{\theta}{P(1-\theta)} \right) \]  
\[ -RT \ln \left( \frac{\theta}{P(1-\theta)} \right) = \Delta H_0 - 0\delta \Delta H - T\Delta S \]  

where \( \Delta G_{\theta,T} \) can be experimentally determined at each \( \theta, T, P \) according to eq 5. The combination of the two \( \Delta G_{\theta,T} \) expressions (eqs 4 and 5) yields eq 6, from which one can derive expressions for fitting isothermal experimental data (in terms of \( P_{\theta,T} \) and isobaric experimental data (in terms \( T_{\theta,P} \)).

An expression in terms of coverage \( \theta_{\max} \) is not possible. The three fitting parameters or metrics are \( \Delta H_0, \delta \Delta H \), and \( \Delta S \). It is generally assumed that these thermodynamic parameters are independent of coverage and temperature. With the proper collection of experimental data (i.e., with variable \( P, T, \theta \) data sets), one can uniquely determine these three metrics. Again, \( \Delta H_0 \) is the adsorption enthalpy (negative value) at zero coverage, \( \delta \Delta H \) is the difference in enthalpy (negative value) between zero and full coverage, and \( \Delta S \) is the adsorption entropy (negative value).

In contrast, the Temkin heterogeneous surface case assumes (i) a uniform distribution of heterogeneous binding sites, and (ii) the binding energy on each site (or type of site) varies linearly over all sites. Uniform distribution means that the surface is divided into a number of uniform elements \( ds \) and the coverage on any particular surface element \( s \) (with binding energy \( \Delta H_s \)) obeys the Langmuir and associated thermodynamic expressions:

\[ \theta_s = \frac{K_P s}{1 + K_P s} \]  
\[ K_s = e^{-\Delta G_s/RT} \]  
\[ \Delta G_s = \Delta H_s - T\Delta S \]  

The linear decrease in the adsorption enthalpy due to surface heterogeneity is expressed as:

\[ \Delta H_s = \Delta H_0 - s\delta \Delta H \]  

In this case, \( \Delta H_0 \) is the largest adsorption enthalpy for the \( s = 0 \) surface element and \( \Delta H_s \) is the smallest enthalphy for the \( s = 1 \) element, \( \delta \Delta H \) is the difference between the two extreme values, and \( s \) ranges from 0 to 1 (i.e., the total number of surface elements is normalized to unity). As an example, consider a heterogeneous surface divided into five elements with \( s = 0, 0.25, 0.50, 0.75, \) and 1, and with binding energies that vary linearly as \( \Delta H_0 = -65 \), \( \Delta H_{0.25} = -62.5 \), \( \Delta H_{0.5} = -60 \), \( \Delta H_{0.75} = -57.5 \), and \( \Delta H_1 = -55 \text{ kJ/mol} \). At a particular pressure, the coverage on each surface element is given by eq 7. It is important to note that \( s \) is simply an index, \( s \neq \theta \), and eqs 10 and 3 are not equivalent.

The observed experimental coverage (i.e., the total coverage on all surface elements) is:

\[ \theta = \int_0^1 \theta_s ds = \int_0^1 \frac{K_P s}{1 + K_P s} ds \]  

Integration gives:
\[
\theta = -\frac{RT}{\delta \Delta H} \ln \left( \frac{1 + K_f P}{1 + K_s P} \right)
\]  
(12)

where \(K_f\) is the binding constant for the strongest surface element, and \(K_s\) is the constant for the weakest element, as given by eqs 8 and 9. The negative sign in eq 12 is typically incorporated into the value of \(\delta \Delta H\), such that \(-\delta \Delta H\) is presented as positive. Unlike the adsorbate interaction case above, this case provides an expression (cf., eq 12) in terms of coverage \(\theta_{P,i}\). The fitting parameters or metrics are still \(\Delta H_0\), \(\delta \Delta H\), and \(\Delta \delta S\), and it is generally assumed that these thermodynamic parameters are independent of coverage and temperature. With the proper collection of experimental data (i.e., with variable \((P, T, \theta)\) data sets), one can uniquely determine these three metrics.

The Temkin midrange approximation results from a simplification of the expressions for the other two cases. For the adsorbate interaction case, a common approximation is made near \(\theta = 0.5\), such that the logarithm term containing the coverage in eq 6 is approximated as zero, cf.:

\[
\ln \left( \frac{\theta}{(1 - \theta)} \right) \approx 0
\]  
(13)

This leads to the following simplified expression:

\[
\theta = \frac{(RT \ln P - \Delta H_0 + T \Delta S)}{\delta \Delta H}
\]  
(14)

The negative sign is typically incorporated into the value of \(\delta \Delta H\), such that \(-\delta \Delta H\) is presented as positive. Similarly, for the heterogeneous surface case, the approximation is made that for midrange coverage the pressure is sufficiently large such that \(K_f P\) is much greater than 1, while \(K_s P\) is much less than 1. Equation 12 then reduces to eq 14.

Historically, this midrange approximation expression has been utilized to demonstrate that for many systems the adsorbate surface coverage varies with the logarithm of pressure. The claim can then be made that the adsorption process follows or obeys the Temkin adsorption model, and that the adsorption enthalpy (or binding energy) varies linearly with coverage (or binding site heterogeneity). However, it appears that what is not appreciated is the fact that the enthalpy or energy terms determined from this approximation always lead to a systematic error in the determined values.29

As we have previously discussed in detail, the Temkin adsorbate interaction case is the most appropriate case to use for describing and fitting data for the adsorption of CO on gold.29 It is important to note that nearly all gold particles and surfaces (for both real-world and model catalysts) exhibit very similar CO adsorption behavior. This includes a number of coverage-dependent observations that would be consistent with the Temkin adsorbate interaction model. Studies almost universally indicate that CO adsorption on gold involves low-coordinate sites.2–15 These are typically understood to be of a limited number of CN = 6 and 7 sites, corresponding to corners (or kinks) and edges (or steps), respectively. As we previously demonstrated, the adsorbate interaction case would be appropriate for a limited number of binding sites with similar energies, and it can account for coverage-dependent behavior.29 Furthermore, we believe that the adsorbate interaction case involving indirect interaction of CO with gold particles (or gold metal surfaces) most accurately describes the physicochemical behavior of the adsorption process and is the best explanation for the collection of experimental results.29 Accordingly, \(\Delta H_0\) represents the intrinsic CO adsorption enthalpy without adsorbate interactions, while \(\delta \Delta H\) is a measure of how the adsorption enthalpy changes with CO coverage and is attributed to adsorbate–substrate electronic interactions between CO and the Au nanoparticles.

Concerning the Temkin heterogeneous surface case, because it assumes a uniform distribution of heterogeneous binding sites, this case does not seem appropriate for nanoparticle catalysts. The Temkin adsorbate interaction model is therefore used below for fitting the CO adsorption on supported gold nanoparticle catalysts.

**EXPERIMENTAL SECTION**

The World Gold Council (WGC) provided the 1.51% Au/TiO\(_2\) and the 4.48% Au/Fe\(_2\)O\(_3\) catalysts. According to the WGC data sheets, the gold particle sizes were \(d = 3.8 \pm 0.8\) nm for Au/TiO\(_2\) and \(d = 3.7 \pm 0.9\) nm for Au/Fe\(_2\)O\(_3\) as determined by TEM. The 1.92% Au/ZrO\(_2\) catalyst (\(d = 1.6 \pm 0.6\) nm by TEM) was prepared by the deposition–precipitation method. First, the support was precipitated from ZrO\(_2\)·8H\(_2\)O (Fluka) at a constant pH of 8.6, aged under reflux conditions for 20 h, washed free of chloride (AgNO\(_3\) test), and then dried at 383 K overnight. The support was then calcined by heating to 923 K in flowing air for 6 h, followed by cooling to room temperature. Gold was deposited on the calcined support at constant pH (0.5 M NaOH aqueous solution, pH = 8.6), filtered, and then dried at 310 K for 15 h.

Each catalyst was pressed into a self-supporting pellet and mounted in a cell that allowed thermal treatment in a controlled atmosphere. Pellet samples were pretreated in situ by reduction in hydrogen gas at 523 K (for Au/TiO\(_2\) and Au/Fe\(_2\)O\(_3\)) or at 423 K (for Au/ZrO\(_2\)) followed by hydration at 298 K. FTIR transmission spectra were collected with a Perkin-Elmer 1760 spectrometer equipped with an MCT detector. A background spectrum (collected before exposure of CO) was subtracted from each sample spectrum. The catalyst samples were cooled with liquid nitrogen and then exposed to a constant pressure of CO according to the following conditions: Au/TiO\(_2\) at 77 K and \(P_{CO} = 3\) mbar; Au/Fe\(_2\)O\(_3\) at 103 K and \(P_{CO} = 0.7\) mbar; Au/ZrO\(_2\) at 90 K and \(P_{CO} = 0.5\) mbar. Spectra were then collected as the samples were allowed to gradually warm to room temperature. All spectra were normalized to the gold content in each pellet before integration of the CO band.

The infrared integrated intensities around 2100 cm\(^{-1}\) were used to measure the CO adsorption (\(S\)) at each temperature, while the spectra at the lowest temperature were used to determine the maximum CO adsorption (\(S_{\text{max}}\)). The CO adsorption coverage was then defined as \(\theta = S/S_{\text{max}}\).

**RESULTS**

Infrared transmission spectra were collected and quantified for the isobaric adsorption of CO on the gold catalysts Au/TiO\(_2\), Au/Fe\(_2\)O\(_3\), and Au/ZrO\(_2\). Illustrative spectra for adsorption on the Au/ZrO\(_2\) catalyst are displayed in Figure 1. The CO pressure was held constant at 0.5 mbar, while the temperature was gradually warmed from 90 K. The integrated peak area (around 2100 cm\(^{-1}\)) at 90 K was used to define the maximum coverage and to normalize the coverage at the higher temperatures. The spectra displayed in Figure 1 are for temperatures from 190 to 277 K, corresponding to CO coverage of \(\theta = 0.84–0.45\), respectively. Spectra with similar
characteristics were collected and quantified for CO adsorption on Au/TiO₂ and on Au/Fe₂O₃, but are not shown for brevity.

The isobaric plot of coverage as a function of temperature is shown in Figure 2a, again for CO adsorption on Au/ZrO₂ (the data from the spectra in Figure 1). Also in Figure 2, the adsorption data have been plotted according to the complete Temkin adsorbate interaction treatment. ΔG was calculated for each coverage-temperature data point using eq 5. Plots of ΔG versus temperature and ΔG versus coverage were then prepared. The data for these three plots were fit simultaneously using eqs 4–6 and the three thermodynamic fitting metrics ΔH₀, δΔH, and ΔS. Because the data for only one isobar were analyzed, the adsorption entropy was fixed to the value determined previously for CO adsorption on an Au/TiO₂ catalyst (cf., ΔS = −142 J/K·mol)²⁹ Excellent fits were then achieved with the values ΔH₀ = −75.3 kJ/mol and δΔH = −39.5 kJ/mol.

The same procedure was utilized for analyzing the data for the other two catalysts. The resulting thermodynamic parameters are listed in Table 1. The ΔH₀ values for these two catalysts are very similar (cf., ΔH₀ = −63.4 and −66.0 kJ/mol for Au/Fe₂O₃ and Au/TiO₂, respectively), with the Au/TiO₂ showing only slightly stronger intrinsic CO binding. Although their underlying supports are different, these two catalysts to the Au/ZrO₂ catalyst, there is a clear difference due to the smaller Au particle size (cf., d = 1.6 nm) and not to the different supports, as we discuss further below.

### APPLICATION OF THE TEMKIN ADSORBATE INTERACTION MODEL

#### a. Real-World Au/TiO₂ Catalyst

To further validate the applicability of the Temkin adsorbate interaction model, the CO adsorption data from a study involving supported gold nanoparticles of a Au/TiO₂ real-world catalyst by Bianchi’s research group were analyzed.²² Particle size was reported to be in the typical range for the deposition—precipitation method, ca. d = 3–5 nm. Infrared spectroscopy (AEIR: absorption equilibrium infrared) was used to quantify the CO adsorption coverage. Two isobars at P = 1 and 10 kPa over a temperature range of T ≈ 300–400 K were reported in Figure 4 of ref 22.

These two isobars are reproduced in Figure 3, along with plots for the analysis using the Temkin adsorbate interaction model. For completeness, a full treatment of the Temkin adsorbate interaction model was used to determine the best set of thermodynamic metrics. ΔG was calculated for each coverage-temperature point using eq 5. The entropy value was set at the value (cf., ΔS = −142 J/K·mol) determined from the analysis of multiple isotherms, as discussed previously.²⁹ The fitting of the three plots (θ vs T, ΔG vs T, and ΔG vs θ) was performed simultaneously with one set of thermodynamic metrics for both pressures (i.e., a total of six curves fit simultaneously). The resulting curves from this fitting procedure are displayed in Figure 3. Taking into account the scatter in the experimental data points, the fits are excellent. The thermodynamic metrics determined from the Temkin model for this data set are given in Table 1 (cf., ΔH₀ = −69.3 and δΔH = −12.2 kJ/mol).
The original authors analyzed the data using a form of the Temkin heterogeneous surface model (cf., eq 12) with the use of binding coefficient expressions \((K_0\) and \(K_1\)) derived from statistical thermodynamics, thereby removing the entropy term and reducing the fitting to just two parameters. From their analysis, they reported energy values for the strongest and weakest binding sites of \(E_0 = -74\) and \(E_1 = -47\) kJ/mol, respectively. Using their Temkin heterogeneous surface expression, we were also able to reproduce their reported adsorption energies (cf., \(E_0 = -73\) kJ/mol and \(E_1 = -48\) kJ/mol). Additionally, we used our heterogeneous surface expression (cf., eq 12) to fit this data set. Holding \(\Delta S\) constant (cf., \(-142\) J/K-mol), our Temkin heterogeneous case yielded enthalpy values \((\Delta H_0 = -75.0\) and \(\Delta H_1 = -51.6\) kJ/mol, respectively) that agree with the results using Bianchi’s expression that utilizes statistical thermodynamic relationships for the binding coefficients. As we have previously demonstrated, the Temkin heterogeneous surface case always yields larger \(\Delta H_0\) and \(\Delta S\) values as compared to the Temkin adsorbate interaction case.\(^{29}\) The heterogeneous surface case also requires a uniform distribution of heterogeneous sites, which is rather unlikely for real nanoparticle catalysts. Furthermore, as we have previously discussed in detail, the adsorbate interaction case is most consistent with the current body of experimental and theoretical evidence.\(^{29}\)

**b. Model Au/TiO\(_2\) Catalysts I.** Meier and Goodman reported a surface science study for CO adsorption on Au clusters supported on a crystalline TiO\(_2\) surface, which we describe as model Au/TiO\(_2\) catalysts.\(^{21}\) By varying the deposition of gold, measured as Au monolayer equivalent (MLE), they prepared Au clusters of various sizes, cf., \(d = 1.8, 2.5, \) and 3.1 nm. Infrared reflection absorption spectroscopy (IRAS) was used to quantify the adsorption coverage, and the pressure and temperature ranges were \(P = 10^{-2} - 10^{-8}\) Torr and \(T = 130 - 265\) K. Because the data showed a coverage-dependent binding enthalpy, a Clausius–Clapeyron analysis of isosteres (i.e., constant coverage) was utilized to determine enthalpies.

From the reported isotherms (Figures 3, 7, and 11 from ref 21), we extracted isobaric data sets for two pressures for each cluster size. This was the most effective way of using as much of the original data to cover the largest range of CO coverage. Regarding the normalization of the coverage, for the \(d = 3.1\) nm data, the coverage is as reported by the authors. For the other two particle sizes, the data sets were normalized using the lowest temperature and highest pressures to determine an \(S_{\text{max}}\) according to eq 2.

![Graph A](image1)

**Figure 3.** Application of the Temkin adsorbate interaction model to the CO adsorption on Au/TiO\(_2\) catalysts from ref 22. The isobaric coverage data (A) comes from adsorption equilibrium infrared spectra. \(\Delta G\) was calculated for each \((\theta, T)\) point in (A) according to the Temkin adsorbate interaction expression, eq 5. The curves in (A)–(C) are from the fitting of all of the data to one set of thermodynamic metrics \((\Delta H_0, \delta\Delta H, \text{ and } \Delta S)\) according to the Temkin adsorbate interaction model. See Table 1 for all fitting values.

<table>
<thead>
<tr>
<th>System Studied ((d \text{ in nm}))</th>
<th>(\Delta H_0)</th>
<th>(\delta\Delta H)</th>
<th>(\Delta S)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>This Work</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Au/ZrO(_2) ((d = 1.6))</td>
<td>75.3</td>
<td>93.5</td>
<td>142</td>
</tr>
<tr>
<td>Au/Fe(_2)O(_3) ((d = 3.7))</td>
<td>63.4</td>
<td>31.0</td>
<td>142</td>
</tr>
<tr>
<td>Au/TiO(_2) ((d = 3.8))</td>
<td>66.0</td>
<td>35.0</td>
<td>142</td>
</tr>
<tr>
<td><strong>Real-World Catalysts(^{22})</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
| Au/TiO\(_2\) \((d = 3)\)        | 69.3 \((74)\)  | 12.2 \((27)\)  | 142 
| **Model Au/TiO\(_2\) Catalysts I\(^{21}\)**| | | |
| (i) \((d = 3.1)\)              | 64.0 \((52.3)\) | 22.0 \((28.5)\) | 120       |
| (ii) \((d = 2.5)\)             | 66.0 \((76.1)\) | 17.0 \((16.0)\) | 140       |
| (iii) \((d = 1.8)\)            | 74.0 \((68.2)\) | 23.0 \((6)\)   | 160       |

\(^{29}\) These are approximate values based upon the data sets in Figures 5, 9, and 12 of ref 21; see text for details.
Plots of the normalized data and fits from the Temkin adsorbate interaction model are shown in Figure 4. Cluster size and pressures are given in the figure (note that the two pressures differ by an order of magnitude). The two isobars for each Au cluster size were fit simultaneously using the same set of thermodynamic metrics, thereby yielding unique entropy values. The value of the entropy term affects the separation of the two isobars for each cluster size.

The resulting thermodynamic metrics for the Temkin adsorbate interaction model are given in Table 1. The enthalpy at zero coverage varies with cluster size as $-\Delta H_0 = 64.0, 66.0,$ and $74.0 \text{ kJ/mol}$ for $d = 3.1, 2.5,$ and $1.8 \text{ nm}$, respectively. These values can be compared to the values reported by the authors (from a Clausius–Clapeyron analysis of isosteres) as $-\Delta H_0 = 52.3 \pm 2.9, 76.1 \pm 4.5,$ and $68.2 \pm 4.5 \text{ kJ/mol}$, respectively. The errors reported here have been extracted from Figure 13 of ref 21. The agreement in the range of values is pretty good, especially in light of the scatter in the original data and the large error bars. In contrast to a jump in $\Delta H$ at $d = 2.5 \text{ nm}$ reported by the authors ($cf., \Delta H_0 = -76.1 \text{ kJ/mol}$), the results from the Temkin model gives rise to a linear relationship between $\Delta H_0$ and Au cluster size. This linear trend seems reasonable and agrees with the results from another Au/TiO$_2$ model catalysts study that also displays a trend in $\Delta H_0$ with particle size; see below.$^{23}$ Table 1 contains the values for $\delta \Delta H$, which are all very similar and do not show a trend with cluster size. These values can be compared to the literature values that have been estimated from data in Figures 5, 9, and 12 of ref 21. It is interesting to note that the literature value of $\delta \Delta H = 0 \text{ kJ/mol}$ for the $d = 1.8 \text{ nm}$ Au clusters would suggest that the adsorption data should fit a Langmuir expression. However, the data cannot be fit using the Langmuir expression. Instead, the Temkin adsorbate interaction model with an enthalpy that varies with coverage accurately represents this data. Last, while the original analysis did not yield an adsorption entropy, this Temkin treatment yields entropy values of $-\Delta S = 120, 140,$ and $160 \text{ J/K mol}$ for $d = 3.1, 2.5,$ and $1.8 \text{ nm}$, respectively. Thus, there is an interesting and somewhat expected trend in $\Delta S$ with $\Delta H_0$. As the particles become smaller and the binding becomes stronger, the adsorption entropy increases in magnitude, indicating that as the CO is more tightly bound it therefore has less entropy.

c. Model Au/TiO$_2$ Catalysts II. Another surface science study on Au/TiO$_2$ model catalysts was reported by Behm’s research group.$^{25}$ By varying the amount of deposited Au, they generated particles of different size, $cf., d = 2, 3,$ and $4 \text{ nm}$. The CO adsorption coverage was quantified using infrared spectroscopy, in this case, polarization-modulation infrared reflection–absorption spectroscopy (PM-IRAS). The pressure of CO was held constant at $10 \text{ mbar}$, and the temperature was varied, $T = 300\text{–}400 \text{ K}$. Isobars for the three sizes were reported in Figures 1 and 2 of ref 23. The authors determined binding enthalpies based upon the Temkin treatment developed by Bianchi.$^{26}$ Again, this treatment is equivalent to the heterogeneous surface case, eq 12, with the use of binding coefficient expressions ($K_0$ and $K_1$) derived from statistical thermodynamics. The authors reported binding energies that decrease in magnitude with increasing Au particle size.

The isobars for this data set are reproduced in Figure 5, along with plots for the analysis using the Temkin adsorbate interaction model. Because only one pressure for each particle size was reported, we used a full treatment of the Temkin adsorbate interaction model to determine the best set of thermodynamic metrics. In other words, the fitting for the three plots of $\theta$ versus $T$, $\Delta G$ versus $T$, and $\Delta G$ versus $\theta$ was performed simultaneously with one set of thermodynamic parameters for each particle size. $\Delta G$ was calculated for each coverage-temperature point using eq 5. The curves in Figure 5 are from this fitting procedure. The fits are very good, particularly considering the scatter in the original data points.

The thermodynamic metrics based upon this fitting are reported in Table 1. Because there is only one data set for each particle size, a unique value of the adsorption entropy cannot be determined. We therefore used $\Delta S = -142 \text{ J/K mol}$, as determined previously from multiple isotherms.$^{29}$ For comparison purposes, Table 1 also includes the values reported by

Figure 4. Application of the Temkin adsorbate interaction model to CO adsorption data on Au/TiO$_2$ model catalysts I from ref 21. The Au particle size is reported as monolayer equivalent gold (MLE) and as average diameter (nm). The coverage data come from infrared reflection absorption spectra. For each particle size, two pressures were selected to span the largest coverage range; see the text for details. The curves are from the fitting of each particle size to one set of thermodynamic metrics ($\Delta H_0$, $\delta \Delta H$, and $\Delta S$); see Table 1 for values.
The agreement in $\Delta H_0$ values is excellent despite using different Temkin cases. Some of this may be artificial because our entropy term is held constant for the three particle sizes. From the Temkin analysis above for Goodman’s data set of similar Au/TiO$_2$ model catalysts, we determined a trend in entropy with enthalpy. To test for trends in this data set, we imposed a reasonable variation in entropy with enthalpy and particle size ($\Delta S = -150, -130,$ and $-110$ J/K mol for smallest to largest particle size, respectively). Temkin fitting using these entropy values produced enthalpy values of $\Delta H_0/\delta \Delta H = 78/24, 63/10,$ and $52/4$ kJ/mol for smallest to largest particle size, respectively. Thus, whether $\Delta S$ is held constant or allowed to vary in a reasonable way, the trend in enthalpy still stands: $\Delta H_0$ increases in magnitude with decreasing particle size, in very good agreement with the other Au/TiO$_2$ model catalyst analysis above. For these model catalysts, $\delta \Delta H$ also increases in magnitude with decreasing particle size.

### DISCUSSION

As demonstrated by the fits in Figures 2−5, the Temkin adsorbate interaction model accurately represents the data for the adsorption of CO on various gold real-world and model catalysts. For these rather different catalysts, the intrinsic enthalpy without adsorbate interactions varies as $-\Delta H_0 = 63−75$ kJ/mol. These values are in excellent agreement with previous enthalpy determinations, which vary from $(-)62−76$ kJ/mol as listed in Table 1. Most of these catalysts utilize TiO$_2$ as the support; however, there does not appear to be a significant support effect on $\Delta H_0$ provided similar particle sizes are examined. For example, the Au/Fe$_2$O$_3$ (with $d = 3.7 \pm 0.9$ nm) and the Au/TiO$_2$ ($d = 3.8 \pm 0.8$ nm) catalysts from this study have essentially the same Au particle size and very comparable $\Delta H_0$ values (cf., $-63.4$ and $-66.0$ kJ/mol, respectively). Most significant, $\Delta H_0$ does appear to vary approximately linearly with gold particle size, as displayed in Figure 6.

As was previously discussed in detail, CO binds to two types of low-coordinate gold sites: $CN = 6$ corner atoms and $CN = 7$ edge atoms. Using the Wulff construction, Weststrate et al. have estimated the abundance of these low-coordinate sites relative to the total number of surface atoms for gold particles with $d = 1−4.6$ nm. On the basis of their results (cf., Table 3 of ref 14), we have included a plot of the percent of gold corner and edges atoms to total surface atoms for each particle size; see text for details.  

![Figure 5](image_url)

**Figure 5.** Application of the Temkin adsorbate interaction model to the CO adsorption on Au/TiO$_2$ model catalysts II from ref 23. The particle size is reported as monolayer gold (ML) and as average diameter (nm). The isobaric ($P = 10$ mbar) coverage data (A) come from polarization-modulation infrared reflection−absorption spectra. $\Delta G$ was calculated for each ($\theta, T$) point in (A) according to the Temkin adsorbate interaction expression, eq 5. The curves in (A)−(C) are from the fitting of all of the data, for each particle size, to one set of thermodynamic metrics ($\Delta H_0, \delta \Delta H,$ and $\Delta S$) according to the Temkin adsorbate interaction model; see Table 1 for values.

![Figure 6](image_url)

**Figure 6.** Summary of the adsorption enthalpy at zero CO coverage plotted (points) as a function of the gold particle diameter. The values are listed in Table 1, and the references for the literature data are (a) ref 22, (b) ref 21, and (c) ref 23. The curves are plots of the percent of gold corner and edges atoms to total surface atoms for each particle size; see text for details. 

As was previously discussed in detail, CO binds to two types of low-coordinate gold sites: $CN = 6$ corner atoms and $CN = 7$ edge atoms. Using the Wulff construction, Weststrate et al. have estimated the abundance of these low-coordinate sites relative to the total number of surface atoms for gold particles with $d = 1−4.6$ nm. On the basis of their results (cf., Table 3 of ref 14), we have included a plot of the percent of corner and edge sites as a function of gold particle size in Figure 6. The fraction of interface sites between the Au particle and support was not included. As expected, the distribution of corner and edge sites changes with Au particle size. Over this particle size range, as the particle size decreases, the percent corner sites continually increases, while the percent edge sites increases and then decreases for particles smaller than $\sim 2$ nm. Interestingly though, the sum of the two types of low-coordinate sites is
effectively linear over this particle size range \((\text{cf.}, \sim 1-5 \text{ nm})\). These distributions are consistent with those published by Norskov et al. for “free” sites, that is, corner and edge sites not including the Au-support interface.\(^5\)\(^3\) It should be noted that the two scales in Figure 6, \(\Delta H_0\) and \% corners and edges, have simply been aligned to cause the line for \% corners and edges to pass through the \(\Delta H_0\) data points.

Therefore, the intrinsic adsorption enthalpy \(\Delta H_0\) correlates very well with the sum of corner and edge sites. This result can be interpreted as follows. For very small particles, for example, \(d = 1 \text{ nm}\) with 40\% of all Au surface atoms being \(\text{CN} = 6\) corner sites and no edge sites, the enthalpy would be due to binding to corner sites (with \(-\Delta H_0 \approx 78 \text{ kJ/mol}\)). For larger particles, for example, \(d = 4 \text{ nm}\) with only 3\% corner sites and \(\sim 19\% \text{ CN} = 7\) edge sites, the enthalpy would reflect binding to mostly the edge sites (with \(-\Delta H_0 \approx 63 \text{ kJ/mol}\)). For particle sizes between these limits, the enthalpy would be some type of average of these two based upon the relative abundance of corner and edge sites. The nearly linear distribution in Figure 6 then reflects these averages. It is important to note that each particle “size” is actually the average of a distribution of particles. Interestingly, when the percent of corner and edge sites equals zero, the \(\Delta H_0\) value is predicted to be \(-44 \text{ kJ/mol}\), corresponding to binding to the \(\text{CN} = 8\) or 9 terrace sites. This is a reasonably small value, reflecting the observation that CO does not chemisorb to “flat” gold surfaces with \(\text{CN} = 8\) or 9 sites.\(^6\)\(^\text{16}\)

The linear trend with particle size also suggests that the corner and edge sites on Au nanoparticles are not isolated but instead are coupled. Previously, we demonstrated that the Temkin adsorbate interaction model fits a distribution of two coupled binding sites, with the resulting thermodynamic metrics being an average of the adsorption enthalpy for the two sites.\(^9\) This is consistent with Figure 6. This idea of coupled binding sites is further supported by infrared spectroscopy studies from Boccuzzi’s research group.\(^5\)\(^\text{16}\) They performed a thorough vibrational analysis for the adsorption of CO on various Au catalysts. Curve fitting of individual CO infrared spectra produced two peaks for CO bound to two sites, corners and edges. Analysis involving CO isotopes indicated that these Au–CO binding sites are not isolated but are coupled.\(^5\)\(^\text{16}\) Similarly, Weststrate et al. investigated CO adsorption on model Au catalysts using high-resolution photoemission spectroscopy of the Au 4f levels.\(^14\) Their results indicate that the CO adsorbs strongly on \(\text{CN} = 6\) sites (small particles) and less strong on \(\text{CN} = 7\) sites (larger particles). For small particles, the adsorption of CO affects the photoemission spectrum of all Au atoms in the particle.\(^14\) This would suggest that the Au binding sites are interacting or coupled in terms of CO adsorption.

Concerning the other Temkin metrics for these catalysts (see Table 1), the change in adsorption enthalpy with CO coverage varies as \(-\delta \Delta H = 7-40 \text{ kJ/mol}\). As mentioned above, \(\delta \Delta H\) is an adsorption metric related to the adsorbate–substrate electronic interaction and how this interaction changes with surface coverage. For these varied data sets, there is no obvious trend in \(\delta \Delta H\), and the variation in \(\delta \Delta H\) values is probably due to support effects and/or differences in preparation methods and particle size distributions. It does appear, however, that those catalysts with the largest (magnitude) values of \(\delta \Delta H\) (\(\text{cf., this work and model catalysts I}\)) are for data sets that extend to fairly low temperatures and may therefore reflect contributions due to physisorption at the very lowest temperatures. Regarding the adsorption entropy, it varies as \(-\Delta S = 120-160 \text{ J/K.mol}\). While the data sets are limited, the determined values do show a trend with \(\Delta H_0\). In particular, stronger binding leads to larger (negative) adsorption entropies. Future experiments will focus on learning more about the \(\delta \Delta H\) and \(\Delta S\) adsorption metrics and how they can be used to characterize nanoparticle catalysts.

\section*{CONCLUSION}

The adsorption of CO on the real-world catalysts Au/TiO\(_2\), Au/Fe\(_2\)O\(_3\), and Au/ZrO\(_2\) was examined under isobaric experimental conditions, and the adsorption coverage was measured using infrared transmission spectroscopy. The Temkin adsorbate interaction model accurately represented the adsorption data on these real-world gold catalysts. A full thermodynamic treatment of the Temkin adsorbate interaction model for the isobaric data involved three plots: coverage versus temperature, \(\Delta G\) versus temperature, and \(\Delta G\) versus coverage. These plots and the corresponding fits demonstrated a certain self-consistency of the Temkin adsorbate interaction model. Because each plot depends on the thermodynamic metrics in slightly different ways, unique and internally consistent thermodynamic values were determined from the adsorption data sets.

Additionally, we used this new treatment of the Temkin model to fit the data sets for the adsorption of CO on another Au/TiO\(_2\) real-world catalyst, and on gold particles of model Au/TiO\(_2\) catalysts (having different particle sizes) from two independent studies. The model fits the experimental data very well and produced meaningful thermodynamic metrics of enthalpy and entropy, which agreed with previous reports. In particular, the intrinsic adsorption enthalpy at zero CO coverage varies as \(-\Delta H_0 \approx 63-75 \text{ kJ/mol}\) and displays a linear trend with Au particle size. We suggest that the trend in this enthalpy metric reflects the relative contribution of both \(\text{CN} = 6\) and 7 sites. For example, small particles would have more \(\text{CN} = 6\) corner sites and stronger binding (\(\text{cf., } -\Delta H_0 \approx 78 \text{ kJ/mol}\)), while larger particles would have more \(\text{CN} = 7\) edge sites and weaker binding (\(\text{cf., } -\Delta H_0 \approx 63 \text{ kJ/mol}\)). Furthermore, because the data sets can be represented by the Temkin adsorbate interaction model and the \(\Delta H_0\) metric displays a linear trend with particle size, we suggest that the two binding sites are coupled in terms of their CO adsorption energetics.

The Temkin adsorbate interaction model appears to be most consistent with the physicochemical behavior and experimental data for CO adsorption on gold as thoroughly discussed previously. This new treatment of the Temkin adsorption model is straightforward and applicable to both isothermal and isobaric data sets. It provides meaningful thermodynamic metrics of enthalpy and entropy, which can be used to characterize and explain differences between various catalysts. The model should also be applicable to the adsorption of other small molecules on metal surfaces and particles that show coverage-dependence.

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**Notes**

The authors declare no competing financial interest.
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(32) Because a distribution of particle sizes was reported in ref 22 (cf., d = 3–5 nm), we chose the smallest diameter of 3 nm for this data set in Figure 6.