## Trinity University Digital Commons @ Trinity

Understanding by Design: Complete Collection

Understanding by Design

Summer 6-2013

# Take a Chance on Probabiliy - 7th grade

Melanie R. Webb *Trinity University*, melanierwebb@gmail.com

Follow this and additional works at: https://digitalcommons.trinity.edu/educ\_understandings Part of the <u>Education Commons</u>

#### **Repository Citation**

Webb, Melanie R., "Take a Chance on Probabiliy - 7th grade" (2013). *Understanding by Design: Complete Collection*. 289. https://digitalcommons.trinity.edu/educ\_understandings/289

This Instructional Material is brought to you for free and open access by the Understanding by Design at Digital Commons @ Trinity. For more information about this unie, please contact the author(s): melanierwebb@gmail.com. For information about the series, including permissions, please contact the administrator: jcostanz@trinity.edu.

# **UNDERSTANDING BY DESIGN**

# Unit Cover Page

Unit Title: Take a Chance! On Probability

Grade Level: 7<sup>th</sup> Grade Pre-AP

Subject/Topic Area(s): Independent, Dependent, Experimental, and Theoretical Probability

Designed By: Melanie Webb

Time Frame: 8 – 10 days

School District: North East ISD

School: Jackson Middle School

School Address and Phone: Jackson Middle School 4538 Vance Jackson San Antonio, TX 78230 Phone: 210-356-4400

Brief Summary of Unit (Including curricular context and unit goals):

The goal of this unit is for students to understand that probability is a measure that we use to make predictions about future events. Whereas some outcomes are independent of one another, others are dependent on the outcome of previous events, which affects the probability.

Throughout the unit, students will explore probabilities through experimental and theoretical situations and problems.

The unit culminates with the students creating what they perceive to be a fair and fun game of chance.

Some supplementary materials were collected and adapted from many teachers in North East Independent School district.

# Take a Chance! on Probability

# 7<sup>th</sup> Grade Pre-AP

	Stage 1 – Desired Res	sults							
Standards	•	Transfe	er						
	Students will independently use the	ir learning	y to						
TEKS 7.10 The student	Create a game of chance of the	heir cho	pice that uses knowledge of						
recognizes that a physical	probability to entertain and amuse.								
or mathematical model									
(including geometric) can		Meanin	g						
be used to describe the	Understandings	Essen	tial Questions						
experimental and	Students will understand that	•	How can theoretical and						
theoretical probability of	<ul> <li>Real world experiments,</li> </ul>	e	experimental probabilities be						
real-life events. The	trials, and simulations are	L	used to make predictions or						
student is expected to:	used to predict the		draw conclusions?						
(A) construct sample	probability of a given event								
spaces for simple or	probability of a given event.	•	n what situations can the						
composite experiments.	Chance has no memory		outcome of one event affect						
and	For reported trials of a	t	he outcome of another?						
TEKS 8 11 The student									
applies concepts of	simple experiment, the	•	How can we use the data to						
theoretical and	outcome of prior events has	i	nterpret events in the physical						
experimental probability to	no effect on the next.	١	world and our society?						
make predictions. The									
student is expected to	<ul> <li>The experimental</li> </ul>	How can understanding							
$(\Delta)$ find the probabilities of	probability or relative	F	probability help someone win a						
dependent and	frequency of outcomes of	Ç	game of chance?						
independent events:	an event can be used to								
(B) use theoretical	estimate the exact								
probabilities and	probability of an event								
experimental results to	probability of all event.								
make predictions and									
decisions; and	Δ	cauisit	ion						
(C) select and use	Knowledge		Skills						
different models to	Students will know		Students will be able to						
simulate an event.	<ul> <li>Probabilities are fractions</li> </ul>		<ul> <li>Construct and use tree</li> </ul>						
	between 0 and 1 derived from	า	diagrams for describing						
Adopted TEKS 2013	modeling real world experime	nte	relatively small sample						
	modeling real world experiments relatively small sample								
7.6 The student applies			spaces and computing						
mathematical process	• A probability of 0 means an probabilities, as well as for								
standards to use	outcome has 0% chance of visualizing why the number								
probability and statistics to	happening and a probability of 1 of outcomes can be								
describe or solve	means that the outcome will extremely large.								
problems involving	happen 100% of the time. A • Use simulations to collect								
proportional relationships.	probability of 50% means and	avan	data and estimate						
The student is expected	probability of 50% means an even data and estimate								

to:	chance of the outcome occurring.	probabilities for real
(A) represent sample	The probabilities of every	situations that are sufficiently
spaces for simple and	outcome in a sample space should	complex that the theoretical
compound events using	add to 1	probabilities are not obvious
lists and tree diagrams	Sometimes the outcome of one	Calculate probability for
(B) select and use	event does not affect the outcome	simple compound
different simulations to	of another event. (This is when the	independent and dependent
represent simple and	or another event. (This is when the	independent, and dependent
and without technology	Competing a the subserves of another	Performe over evine entrel triale
(C) make predictions and	• Sometimes the outcome of one	• Perform experimental thats
determine solutions using	event does affect the outcome of	to find experimental
experimental data for	another event. (This is when the	probability.
simple and compound	outcomes are called dependent.)	Compare experimental and
events	<ul> <li>Experimental probability</li> </ul>	theoretical probability
(D) make predictions and	approaches theoretical probability	
determine solutions using	when the number of trials is large.	
theoretical probability for		
simple and compound		
(E) find the probabilities of		
a simple event and its		
complement and describe		
the relationship between		
the two		
(H) solve problems using		
qualitative and		
quantitative predictions		
and comparisons		
from simple experiments		
(I) determine		
theoretical probabilities		
related to simple and		
compound events using		
data and sample spaces		

### Stage 2 – Evidence

#### Performance Task

Students will demonstrate meaning-making and transfer by...

Take a Chance!

Students will create a game of chance using at least two types of probability in groups or individually, no more than 3 to a group. The game must require no skill to play. They will write a descriptive essay describing their game's rules, and how to play, as well as discussing the probabilities of the turns, addressing the theoretical probability that they designed and then experimenting with their game to show any difference with the experimental probability and how that might affect outcome.

Other Evidence (e.g., formative) Exit Slips, Class Assignments

#### Stage 3 – Learning Plan

-----

Pre-Assessment

How will you check students' prior knowledge, skill levels, and potential misconceptions?

Pre-test over Simple Probability and Tree Diagrams

HW: Watch and complete handout on video notes/vocabulary for sample spaces, tree diagrams, and simple probability.

Learning Activities	Progress Monitoring
<u>Day 1:</u>	(e.g., formative data)
Learning Goal: Students will be able to construct sample spaces.	
Students will use sample spaces to find probability of desired events. Warm-Up: Card Sort "Impossible, Maybe or Certain?" Given cards with different fractions, percents, scenarios, words, and pictures, students will sort them into groups with like probabilities.	Observe Warm- Ups/Share
Lesson: Group exercise Tree Diagrams with Odd One Out (NE Intranet). Discuss independent compound events via tree diagrams. Learning Task: <b>Heads Wins? for assessment</b> HW: Watch and complete handout on video notes/vocabulary for independent/compound events	Collect Heads Wins
Day 2:	
Learning Goal: Students will be able to find probabilities of independent/compound events. Lesson: Using the learning task Heads Wins? to discuss <u>probability</u> of compound events occurring. Then complete Passing without Studying Part 1. <i>Essential Question: In what situations can the outcome of one event</i>	
affect the outcome of another?	Collect Acciment
compound events	Collect Assignment
Exit Ticket. 3 Compound Event probabilities. HW: Watch and complete handout on video notes/vocabulary for dependent events	Exit ticket for quick check
Day 3: Learning Goal: Students will be able to find probabilities of dependent events.	
Warm-Up: Dependent or Independent. Given 3 scenarios, students will decide if the events are Independent or Dependent.	

Lesson: With a bag full of marbles discuss probability of events occurring if marbles are selected without replacement. Discuss probability of choosing a marble that has been removed from the bag. The next probability is dependent on the outcome of the first! <i>Essential Question: In what situations can the outcome of one event</i> <i>affect the outcome of another?</i> Learning Task: <b>Sock Drawer Assignment</b> HW: Watch and complete handout on video notes/vocabulary for Theoretical v Experimental Probability.	Collect Sock Drawer.
<ul> <li><u>Day 4:</u></li> <li>Learning Goal: Students will understand the difference between theoretical and experimental probability. Students will perform experiments and use the results to predict probabilities for future events.</li> <li>Lesson: With a bag of two color counters, shake it up and spill the contents. Ask the students how many they think would land on yellow (answer should about half). Is this what the experiment shows? Repeat trials, as the experiments show different result, adjust probability. Predict what would happen if you performed the experiment with 100 color counters of 4500 counters. How would we decide this?</li> <li><i>Essential Questions: How can we use theoretical and experimental probabilities to make predictions or draw conclusions? How can we use the data to interpret events in the physical world and our society?</i></li> <li>Learning Task: It's a Boy!</li> <li>Exit Ticket: Why aren't half the babies always boys?</li> </ul>	Collect It's a Boy! Exit Ticket for quick check
<ul> <li><u>Day 5:</u></li> <li>Learning Goal: Students will understand the difference between theoretical and experimental probability. Students will perform experiments and use the results to predict probabilities for future events.</li> <li>Lesson: Passing Without Studying Part 2, Simulated. Revisit the same situation with the previous discussion from Day 2, except this time, using a deck of cards, see how the quiz turns out this time.</li> <li><i>Essential Questions: How can theoretical and experimental probabilities be used to make predictions or draw conclusions? How can we use the data to interpret events in the physical world and our society?</i></li> <li>Learning Task: <b>Probability graphing.</b> Students will flip a coin and record their results on a table and graph as they go to see if the experimental probability approaches the theoretical probability of</li> </ul>	Collect Probability Graphing

flipping heads.	Collect Sum of the
HW: Finish Learning Task	Dice
Day 6:	
Learning Goal: Students will apply probability to situation/problem	
stations.	
Lesson: The Sum of the Dice – What makes a game fair?	
Essential Questions: How can understanding probability help someone	
win a game of chance?	
Learning Task: Probability Figures (NE Intranet), Score 2 (NE	
Intranet),	
HW: Come to class tomorrow with idea for Performance Task Game	
Day 7:	
Learning Goal: Students will create a game using probability.	
Lesson: Go over rubric and expectations for probability game.	
Essential Questions: How can understanding probability help someone	
win a game of chance?	
Learning Task: Work Day on Performance Task	
HW: Complete Game to be ready to participate in class tomorrow	
Day 8:	Summative
Learning Goal: Use knowledge about probability to play and attempt to	assessment Game
win games of chance.	and Essay
Lesson: Using Strategy to play and win each other's games	
Essential Questions: How can understanding probability help someone	
win a game of chance?	
Learning Task: Students will take notes on how their games are played	
and it they are successful. They should record outcomes to use as	
experimental probability data.	
HW: Complete Performance Task Reflection Essay	

#### Take a Chance!

Probability Unit Performance Task assignment sheet

Your task: Create a game that relies entirely on chance to win.

Design a game we will play in class, using what you have learned about probability. You will have one day in class to work on your game, and we will play the games in class the next day.

Possible Options:

- Design a board game like Chutes and Ladders or Candyland
- ✤ Make rules for the roll of two or more dice.
- Make a spinner or die (or dice) that you design with actions or rules to win.

The choice is yours. You will decide the rules for your game. Side note: Try to create at least one rule that includes independent compound or dependent probability.

The math:

- You must give a list of the sample space for your game. For each possible outcome of your game, you will calculate the theoretical probability.
- When we play the game in class, you must play your game and at least one other game by the class and record the outcomes.
  - You will use these outcomes to calculate the experimental probability of each outcome if you were to play again.

The essay: You will be required to turn in a reflection essay about your game that covers this information

- You must describe you game, how to play it with rules included.
- Include your sample space and your initial theoretical probability.
- Describe how your game went when it was played, did you win? Was it fair?
- Include your recording sheet for how often each outcome occurred. Discuss how your experimental probability differs from your initial theoretical probability.
- Answer what you have learned about probability by making this game, what would you do differently next time?

# Take a Chance! Rubric Per: \_\_\_\_\_

Name(s): \_\_\_\_\_

	Needs Improvement (0-5)	Approaching Expectations (6-15)	Meeting Expectations (16- 25)	Exceeding Expectations (26-30)	Total
Product (30pts)	Student did not	Student had completed	Student had	Student had a	
	have a completed	product, though design	completed product	completed product,	
	product by due	was not well thought out	with well explain	with well explained	
	date OR student's	or executed. Students	rules of the game,	rules of their game,	
	product was	may have had difficulty	adhering to the	exhibiting creativity	
	unfinished and	participating.	guidelines specified	while adhering to	
	student was not		on assignment	guidelines	
	able to participate.		sheet.		
Calculations (30pts)	Not included or	Calculations are	Calculations are	Calculations are	
	mostly incorrect	included and mostly	included and	correct, thoughtfully	
	calculations	correct with up to 5	mostly correct with	organized and easily	
		errors. Calculations may	up to 2 errors.	followed. Different	
		be unorganized or	Different types of	types of probability	
		difficult to follow.	probability are	are specified	
			specified		
Essay (30pts)	Not included or	Essay is included, and	Essay is included,	Essay is included, in	
	incomplete	complete, but not	in paragraph form,	paragraph form, well	
		organized in paragraph	and addresses all	written and	
		form. Does not answer	questions listed on	addresses all	
		all required questions.	assignment sheet.	questions listed on	
				assignment sheet	
				thoughtfully.	
Neatness/Organization	(0-2)	(3-5)	(6-8)	(9-10)	
(10pts)	If included,	Product is in pencil,	Product is colored,	Product is colored	
	Product is messy	calculations are not	calculations are	and legible,	
	and work on	easily followed. Essay is	written legibly.	calculations are	
	calculations is not	not written in best	Essay is	written on lined paper	

easily followed.	handwriting or typed.	handwritten legibly	in step by step
Essay is illegible.		or typed.	manner. Essay is
			written in best
			handwriting or typed.

Website Info

Name:								

Period:

### Introduction to Probability Video: Vocabulary and Notes Handout

Watch the video and fill in accompanying notes, definitions, and diagrams. Answer the comprehension questions at the end independently

Simple Probability Definition:

How to find Simple Probability: ------

Example 1: Probability of flipping Heads also written

Example 2: Probability of rolling a multiple of 3 on a six-sided die, \_\_\_\_\_

Desired outcomes:

Possible outcomes:

Sample Spaces Definition:

Sample Space of a coin:

Sample Space of a six-sided die:

When more than \_\_\_\_\_\_ is occurring, a \_\_\_\_\_\_ is an

organizational tool used to create a \_\_\_\_\_.

Example 1: Flipping a coin AND rolling a die:

Example 2: For Breakfast

Website Info

Name:						

Period:

How many different combinations are there when given choices for breakfast?

Drink: {coffee, OJ, milk} Bread: {toast, biscuit} Meat: {sausage, bacon, ham}

Tree Diagram!

Complete the Sample Space: {C/T/S, C/T/Ba, C/T/H, C/Bi/S,

#### Comprehension/ Thinking Questions:

Use the Breakfast information above and your tree diagram for the following questions.

- 1. There are an equal amount of sausage, bacon, and ham sandwiches. What is the probability that you grab a ham sandwich?
- 2. What is the probability that your meal consists of Milk, Toast, and Sausage?
- 3. What is the probability that your sandwich is on a biscuit with either ham or bacon?

Write any questions you have here:

Name:								

Period:

#### Probability of Compound Events Video: Vocabulary and Notes Handout

Independent Events Definition:

Montel is flying from New York to London. The airline has a history of landing on time about 12 out of every 25 flights. This airline also reports to lose luggage only about 5% of the time. Montel wants to know what the probability is that he will arrive on time **and** that the airline does NOT lose his luggage.

Draw a diagram modeling this situation:

Does Event A affect Event B?

If two or more events are \_\_\_\_\_, then the probability of

\_\_\_\_\_ events occurring is the \_\_\_\_\_ of probability of A and probability B.

P (\_\_\_\_\_) = P (\_\_\_\_) P(\_\_\_\_)

Using the tree diagram example from the previous notes:

P(coffee) = P(Toast) = P(Ham) =

Probability of Coffee/Toast/Ham =

Coffee/Toast/Ham is only one (1) combination out of how many total, according to our diagram?

Website Info

Name:							

Period: \_\_\_\_\_

Back to Montel:

What is the probability that his flight will arrive on time? P(A) =

What is the probability that his luggage WILL arrive? P(B) =

What is the probability of both of these events occurring? P (A and B) =

#### Practice Independent Compound Events:

A bag contains 6 black marbles, 9 blue marbles, 4 yellow marbles and 1 green marble. A marble is selected without looking, replaced in the bag, and then a second marble is selected. Find the probability of the following events.

- 1. Selecting a black marble, then a yellow marble.
- 2. Probability (blue, green)
- 3. P(not black, blue)
- 4. P( green, green)

Write any questions you have here:

#### Probability of Dependent Events Video: Vocabulary and Notes Handout

Website Info	Name:
	Period:
Dependent Events Definition:	
In dependent events, the	changes after the initial
event.	
P( A and/then B ) = P()	P()

Example:

Maury only likes red and orange jellybeans. Her bag of jelly beans contains 10 red, 6 green, 7 yellow, and 7 orange jellybeans. After a jellybean is chosen, she eats it. What is the probability of choosing a red jellybean, another red jellybean, and then an orange jellybean?

Find each event separately first, then find the product

P (red) = 
$$\frac{\# of \ red \ jelly \ beans}{total \ jelly \ beans}$$
 = -----  
P (red  $again$ ) =  $\frac{\# of \ red \ jelly \ beans \ left}{total \ jelly \ beans \ left}$  = -----  
P (orange) =  $\frac{\# of \ orange \ jelly \ beans \ left}{total \ jelly \ beans \ left}$  = -----

Is this probability likely?

Practice.

Name:						
	 	 	 	 -		 

Period: \_\_\_\_\_

The principal is choosing two students at random from a class of 25 students to represent our middle school at a city conference about getting kids to go to college. There are 10 girls and 15 boys in the class.

What is the probability that a girl is chosen and then a boy is chosen?
 P(girl) =

P(boy) = Remember one student has already been chosen! =

P(girl, boy) = P(girl) X P(boy after girl) =

- 2. What is the probability that a boy is chosen and then a girl is chosen?
- 3. What is the probability that two girls are chosen?

4. What is the probability that two boys are chosen?

Write any questions you have here:

Website Info

Name:	 			 

Period: \_\_\_\_\_

## Experimental v Theoretical Probability Video: Vocabulary and Notes Handout

Theoretical Probability Definition:

P(event) = -----

We have been working mostly with theoretical probability, using what we know about our possible outcomes to predict the likelihood of an event.

Experimental Probability Defnition:

Experimental P (event) =  $\frac{\# of times event occurs}{total \# of trials}$ 

Example: Rolling a Die

Theoretical Probability of rolling a 1 on a six-sided die: P(1) = ------

Experiment:

Outcome									
1s									
Trials	1	2	3	4	5	6	7	8	9
Probability									

The more trials you perform, the more accurate your data.

Using the experimental probability, how many 1s could you expect (predict) to roll if you rolled the die

50 times?

100 times?

500 times?

## Probability Card Sort.

Teacher Notes: Copy and Cut these cards to be sorted into groups as students see fit, using their mathematical logic. You may give students who need scaffolding five groups: Impossible, Unlikely, Maybe, Likely, and Certain. Feel free to add more situations to create more cards. You may want to include pictures.

Impossible	Maybe	Certain	Good Chance		
Unlikely	Likely	Probable	Small Chance		
Even Chance	No Chance	0%	100%		
10%	25%	50%	75%		
90%	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{3}{4}$		
0.25	0.5	0.75	$\frac{1}{6}$		
5 6	The Rangers will win the World Series	You will have two birthdays this year	If today is Tuesday, tomorrow is Wednesday		
You will meet the President of the United States	You will meet Benjamin Franklin on your way home from school	The sun will rise tomorrow morning	You will go to the beach this summer		
At least one student will be absent tomorrow	At least one student will be absent tomorrow		It will snow this week		
You will watch TV after school	It will rain tomorrow	Add your own word!	Add your own Fraction!		
Add your own decimal!	Add your own percent!	Add your own picture!	Add your own sentence!		

#### Heads wins?

- 1. Suppose you are approached by a classmate who invites you to play a game with the following rules: Each of you take a turn flipping a coin. You toss your coin first, he tosses his coin second.
  - > He gives you 50¢ each time one of the coins lands on tails.
  - > You give him 50¢ each time one of the coins lands on heads.
  - a. Create a tree diagram for the four possible outcomes and probabilities for the two tosses.
  - b. What are the possible outcomes (sample space)?
  - c. What are your winnings for each outcome?
  - d. Would you play the game?
- 2. Your classmate suggests changing the rules to the game to make it interesting. You'll flip first.
  - If you get heads, you give him \$2
  - > If you get tails, he flips his coin.
  - If he gets heads, you give him \$1
  - If he gets tails, he gives you \$2
  - a. Create a tree diagram for the possible outcomes and probabilities. Write your outcomes as fractions, decimals, or percents.
  - b. Who is likely to win this game? Explain your Answer. Would you play this game?

Adapted from Georgia Dept of Education.

## Odd One Out

For each situation, you are given 4 options. Three belong and one does not. Find the odd one out.

1. You have vour pock	2 quarters, 3 et. what cou	3 dimes, and ld they be?	poo	cket.	lf y	ou tak	e 3 c	oins	from			
QQN	<u>ا</u>	QDN							Q			
QQE	)	DDD			Q				N			D
QDE	)	DDN		N D Q D Q						Ň		
Quarte	r Quarter	Nickel		(quarter, dime, nickel)								
Quarte	r Quarter	Dime				(	qua	rter,	dime,	dime	e)	
Quarte	r Dime	Dime					(din	ne, d	dime, o	dime)	)	
Quarte	r Dime	Nickel				(C	luart	er, o	quarte	r, din	ıe)	
Dime	Dime	Dime				(q	uarte	er, c	luarter	, nicł	(el)	
Dime	Dime	Nickel					(dim	e, c	lime, r	nickel	)	
2. Possible S	Sandwiches: C W	eef or riss Ch Bread	Ham	9								
TCW	BCW	BCW HCW			Г			E	3		ŀ	4
TCR	BCR	HCR		С	ç	3	C	2	S		C	S
TSW	BSW	HSW		0				•	U		U	U
TSR	BSR	HSR	W	R	W	R	W	R	W F	R W	R	WR
turkey	Cheddar	Wheat										
Turkey	Cheddar	Rye										
Turkey	Swiss	Wheat										
Turkey	Swiss	Rye				(t	urke	y, b	eef, ha	am)		
beef	Cheddar	Wheat				,			·	,		
Beef	Cheddar	Rye					(che	dda	r, Swis	ss)		
Beef	Swiss	Wheat										
Beef	Swiss	Rye					(w	hea	t, rye)			
Ham	Cheddar	Wheat										
Ham	Cheddar	Rye										
Ham	Swiss	Wheat										
Ham	Swiss	Rye										

### Passing without Studying Part 1

Frank is interested in knowing how likely it is that he will pass a multiple choice quiz without studying. There are ten questions and each question has 4 choices.

- 1. How many questions does Frank need to answer correctly to pass?
- 2. What is the probability that he will guess correctly on the first question?
- 3. What is the probability that he will guess correctly on the first AND second question?
- 4. Continue this pattern to find the probability that he will answer ALL ten questions correctly.
- P (3 Questions):
- P (4 Questions):
- P (5 Questions):
- P (6 Questions):
- P (7 Questions):
- P (8 Questions):
- P (9 Questions):
- P (10 Questions):

Remember, Frank wants to pass this quiz, so he needs \_\_\_\_\_ questions correct. What is the probability Frank will pass the quiz?

Do you think Frank should study?

Exit Ticket Compound Probability

Name:

Period:

1. If a coin is flipped 4 times, what is the probability of getting Tails all 4 times?

2. What is the probability of rolling two even numbers in a row with a six-sided die?

3. What is the probability of flipping heads on a coin and rolling a 3 on a die?

Exit Ticket Compound Probability

Name:

Period:

1. If a coin is flipped 4 times, what is the probability of getting Tails all 4 times?

2. What is the probability of rolling two even numbers in a row with a six-sided die?

3. What is the probability of flipping heads on a coin and rolling a 3 on a die?

Warm – Up: Independent or Dependent?

- 1. A toy bin contains 12 toys, 8 stuffed animals, and 3 board games. Marsha randomly chooses 2 toys for the child she is babysitting to play with. What is the probability that she chose 2 stuffed animals as the first two choices?
- 2. A fruit basket contains 6 apples, 5 bananas, 4 oranges, and 5 peaches. Drew randomly chooses on piece of fruit, eats it, and chooses another piece of fruit. What is the probability that he chooses a banana and then an apple?
- 3. Nick has 4 quarters, 3 dimes, and 2 nickels in his pocket. Nick randomly picks two coins out of his pocket. What is the probability that Nick did not choose a dime either time if he replaced the first coin back in his pocket before choosing a second coin?

Name: Period:

### Warm – Up: Independent or Dependent?

- 1. A toy bin contains 12 toys, 8 stuffed animals, and 3 board games. Marsha randomly chooses 2 toys for the child she is babysitting to play with. What is the probability that she chose 2 stuffed animals as the first two choices?
- A fruit basket contains 6 apples, 5 bananas, 4 oranges, and 5 peaches. Drew randomly chooses on piece of fruit, eats it, and chooses another piece of fruit. What is the probability that he chooses a banana and then an apple?
- 3. Nick has 4 quarters, 3 dimes, and 2 nickels in his pocket. Nick randomly picks two coins out of his pocket. What is the probability that Nick did not choose a dime either time if he replaced the first coin back in his pocket before choosing a second coin?

#### **Passing without Studying Part 2**

Remember Frank? He was trying to pass a quiz without studying. This time, however, we will run trials of an experiment to find his probability of passing the quiz. There are ten questions and each question has 4 choices.

Let a deck of cards represent his answer choices, since there are 4 choices and 4 suits. Let Hearts represent the correct answer. Shuffle the deck, pick a card and record your result. Replace the card and repeat to represent the next question. Do this ten times for the ten questions on the quiz.

Run this experiment 10 – 20 times. Find an average for your results. Does Frank Pass? How does this experimental probability differ from the probability you found previously?

Name:

Period:

#### **Probability Graphing**

To explore the probability of getting heads in a coin toss, run an experiment of 30 trials. Count how many heads you get in 30 trials to investigate how experimental probability changes with each trial. In your table, record how many heads have come up in your experiment, the number of trials you completed, and the experimental probability as a percentage after each trial.

For Example, if your first six trials resulted in Tails, Heads, Tails, Heads, Heads, Heads, your table would look like this:

OUTCOME	Т	Н	Т	Н	Н	Н
HEADS	0	1	1	2	3	4
TRIALS COMPLETED	1	2	3	4	5	6
EXPERIMENTAL PROBABILITY	0%	50%	33%	50%	60%	66%

Record your results below:

OUTCOME										
HEADS										
TRIALS	4	0	2	4	Б	6	7	0	0	10
COMPLETED	I	2	3	4	5	0	1	0	9	10
EXPERIMENTAL										
PROBABILITY										

OUTCOME										
HEADS										
TRIALS COMPLETED	11	12	13	14	15	16	17	18	19	20
EXPERIMENTAL PROBABILITY										

OUTCOME										
HEADS										
TRIALS COMPLETED	21	22	23	24	25	26	27	28	29	30
EXPERIMENTAL PROBABILITY										

Adapted from Georgia Dept of Education

Create a Graph showing the change in the probability as the number of trials is increased.



What did you notice as you performed more trials?

#### The Sum of the Dice

Discuss what you think makes a game fair with a classmate.

Next you will play a game with a partner. In this game, you will roll two dice and receive points based on the sum.

- Person A will receive a point if the sum of the dice is 1, 2, 3, 4, 10, 11, or 12
- Person B will receive a point if the sum is 5, 6, 7, 8, or 9
- A. Before you start playing: Is this game fair? Why or why not?
- B. Roll the dice 10 times and record the points. Who won?
- C. Repeat the game 5 more times. Did your results change?
- D. Create a Bar Graph that displays the number of times the sum occurred on a separate sheet of paper.
- E. What would happen if you played the game with 100 rolls?
- F. Who wins this game more often? Why do you think that is?
- G. Show all the possible sums (sample space). How many are there.
- H. Is there a way to change the rules of the game so that each player has an equal chance to win? Explain

Adapted From Georgia Dept of Education